## CONFIDENTIAL

UNIVERSITI TUN HUSSEIN ONN MALAYSIA

## FINAL EXAMINATION SEMESTER II SESSION 2014/2015

| COURSE NAME | $:$ DATA ANALYSIS |
| :--- | :--- |
| COURSE CODE | $:$ BWA 21003 |
| PROGRAMME | $:$ BWA |
| EXAMINATION DATE | $:$ JUNE 2015/JULY 2015 |
| DURATION | $: 3$ HOURS |
| INSTRUCTION | $:$ ANSWER ALL QUESTIONS |

Q1 (a) Explain two differences between primary data and secondary data.
(4 marks)
(b) List 5 steps of statistical analysis.
(c) Given the SPSS output of ' $m p g$ ' as presented in Table Q1(c) below.

Table Q1(c) Descriptive summary of ' mpg '

|  |  | Statistic | Std. Error |
| :--- | :--- | ---: | ---: |
| mpg | Mean | 20.9231 | .93302 |
|  | 95\% Confidence | Lower Bound | 19.0015 |
|  | Interval for Mean | Upper Bound | 22.8447 |
|  |  |  |  |
|  |  | 20.6026 |  |
|  | M\% Trimmed Mean |  | 21.0000 |
|  |  |  |  |
| Median | 22.634 |  |  |
| Variance | 4.75750 |  |  |
| Std. Deviation | 14.00 |  |  |
| Minimum | 35.00 |  |  |
| Maximum | 21.00 |  |  |
| Range | 6.25 |  |  |
| Interquartile Range | .935 | .456 |  |
| Skewness | 1.793 | .887 |  |

(i) Interpet the skewness of ' $m p g$ '.
(ii) Describe the pattern of kurtosis.
(iii) Interpret the $95 \%$ confidence interval of mean.
(d) Analyse the box plot in Figure Q1(d). Do the diagnostic checking and give your recommendations.


Figure Q1(d) Box Plot of 'mpg'

Q2 (a) In testing the hypotheses $H_{0}: \beta_{1}=0$ and $H_{1}: \beta_{1} \neq 0$, both $F$-test and $t$-test can be used. Show that both tests are algebraically equivalent.
(b) Verify that the total sum of squares (SST) is a decomposition of error sum of squares (SSE) and regression sum of squares (SSR) by showing that the left hand side of the following equation is the same as the right hand side.

$$
\begin{aligned}
& \sum_{i=1}^{n}\left(Y_{i}-\bar{Y}\right)^{2}=\sum_{i=1}^{n}\left(Y_{i}-\hat{Y}_{i}\right)^{2}+\sum_{i=1}^{n}\left(\hat{Y}_{i}-\bar{Y}\right)^{2} \\
& {\left[\text { Hint: } \sum_{i=1}^{n}\left(Y_{i}-\bar{Y}\right)^{2}=\sum_{i=1}^{n}\left[\left(\hat{Y}_{i}-\bar{Y}\right)+\left(Y_{i}-\hat{Y}_{i}\right)\right]^{2}\right]}
\end{aligned}
$$

(6 marks)
(c) A study was conducted to determine the relationship between starting salaries (RM thousands) for recent statistics graduates and their grade point averages in the major course. A linear regression model was fitted to the data and the estimates regression function was obtained. Part of the computer output for the above analysis is given below in Table Q2(c):

Table Q2(c) MINITAB computer output

| ANOVA |  |  |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: | :---: |
| Model | Sum of <br> Squares | df | Mean <br> Square | F | Sig. |  |
| Regression |  | 1 |  | 147.28 | .000 |  |
| Error | 734.9 |  | 40.828 |  |  |  |
| Total | 6748.2 |  |  |  |  |  |

Coefficients

| Model | Unstandardized <br> Coefficients |  | t | Sig. |
| :--- | :---: | :---: | :---: | :---: |
|  | $\beta$ | Std. <br> Error |  |  |
| Constant | -8.42 | 3.395 | -2.48 | 0.011 |
| GPA | 3.007 | 0.2477 | 12.14 | 0.000 |

(i) Complete the ANOVA in Table Q2(c).
(ii) Write the estimated regression function.
(iii) Determine the coefficient of determination for the model and interpret its meaning.

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Q3 (a) Give your comments of the following statements.
(i) Value of $R^{2}$ is close to 1 .
(ii) Value of correlation coefficient is close to zero.
(b) The following table shows the mean speeds of 12 motorcycles and the amount of traffic fines (RM) they pay during a period of a month.

Table Q3(b) Mean speeds and traffic fines

| Mean Speed (km/h) | Trafic fines (RM) |
| :---: | :---: |
| 100 | 300 |
| 120 | 350 |
| 115 | 320 |
| 112 | 315 |
| 108 | 310 |
| 105 | 305 |
| 116 | 340 |
| 121 | 360 |
| 125 | 380 |
| 118 | 345 |
| 115 | 320 |
| 122 | 330 |

Assuming that both mean speeds and the traffic fines are normally distributed.
(i) Obtain the linear regression of the fines against the mean speeds.
(ii) At the signficant level of 0.05 , test the hypothesis that there exists a positive relation of the fines against the mean speeds.
(iii) Find the Pearson correlation coefficient between the mean speeds and fines. Interpet your finding.

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Q4 (a) A QC engineer is testing a power supply used in producing notebook components. The complete table of observed frequencies is as follows:

Table Q4(a) Frequency table of power supply

| Class interval | Observed frequencies $O_{i}$ |
| :---: | :---: |
| $x<4.948$ | 12 |
| $4.948 \leq x<4.986$ | 14 |
| $4.946 \leq x<5.014$ | 12 |
| $5.014 \leq x<5.040$ | 13 |
| $5.040 \leq x<5.066$ | 12 |
| $5.066 \leq x<5.094$ | 11 |
| $5.094 \leq x<5.132$ | 12 |
| $x \geq 5.132$ | 14 |

Test whether the output voltage is adequately described by a normal distribution with mean 5.04 V and standard deviation 0.08 V at a significance level of 0.05 .
(b) Then, the QC engineer took a set of sample data to determine whether the proportions of output of notebook components for two shifts produced by machine A, B and C were the same. The following data were collected:

Table Q4(b) Work shifts and machines

| Shift | Machine |  |  |
| :---: | :---: | :---: | :---: |
|  | A | B | C |
| 1 | 100 | 120 | 180 |
| 2 | 120 | 180 | 100 |

Use a 0.05 level of significance to determine if the proportions of components for shift 1 are the same for all three machines.

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Q5 Three set of five mice were randomly selected to be placed in a standard maze but with different color doors. The response is the time required to complete the maze as seen below. Refer to the SPSS output as given in Appendix 1.

Table Q5 Time required to complete the maze

| Colour | Time |  |  |  |  |
| :--- | :---: | :---: | :---: | :---: | :---: |
| Red | 9 | 11 | 10 | 9 | 15 |
| Green | 20 | 21 | 23 | 17 | 30 |
| Black | 6 | 5 | 8 | 14 | 7 |

(a) Briefly explain on the normality assumption based on Normal P-P plot of maze time for each different colour doors.
(b) Conduct a test whether the variances are equal by using 0.01 level of significant.
(c) Perform the appropriate analysis to test if there is an effect due to door colours. Then, if there is a difference in the mean times to complete the maze based on the door colours, perform Tukey-Kramer multiple comparison test. Use 0.01 level of significant for both analysis.
(13 marks)

## FINAL EXAMINATION

| SEMESTER $/$ SESSION | : SEM II / 2014/2015 | PROGRAMME | $: 2$ BWA |
| :--- | :--- | :--- | :--- |
| COURSE | DATA ANALYSIS | COURSE CODE | $:$ BWA 21003 |

## APPENDIX 1(1)



## Oneway

Ifest of Homogentity of Variances
Haze Time

| Levene <br> Statistic | off | df2 | 8ig. |
| ---: | ---: | ---: | ---: |
| .6522 | 2 | 12 | .5384 |

ANONA
Maze Time

|  | Sum of |  |  |  |  |
| :--- | ---: | ---: | ---: | ---: | ---: |
| Between Groups | 2 | Squares | Mean Square | F | 8ig. |
| Within Groups | 12 | 565.7333 | 282.8667 | 20.0142 | .0002 |
| Total | 14 | 735.3300 | 14.1333 |  |  |

## APPENDIX 1(2)

## Post Hoc Tests

| Multiphe Companisonts |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| Dependent Variable: Maze TimeTukey HSD |  |  |  |  |  |
| (0)Door Colar (3) Door Color | $\qquad$ | Std. Error | Sig. | 99\% Confidence intertal |  |
|  |  |  |  | Lower Bound | Upper Bound |
| Black | - 2.8000 | 2.3777 23777 | . 0012 | -198836 | -2.9484 |
| Green Red | 11.4000 | 2.3777 | 4879 | -5.6836 | 11.2836 |
| Black | $14.2000{ }^{\circ}$ | 2.3777 23717 | . 0012 | 2.9164 | 19.8836 |
| Black Red | -28000 | 2.3777 | 0002 | 5.7164 | 22.6838 |
| Green | -14.2000* | 23777 23777 | 4879 | -11.2836 | 5.6838 |
|  |  |  |  |  | . 5.7164 |

## Homogeneous Subsets

Maze Thne

| Tukey HSD |  |  |  |
| :--- | ---: | ---: | ---: |
| 2 |  |  |  |
| Doar Color | N | Subset for alpha $=.01$ |  |
| alack |  | 1 | 2 |
| Red | 5 | 8.0000 |  |
| Green | 5 | 10.8000 |  |
| Big. | 5 |  | 22.2000 |

means for groups in homogeneous subsets are displayed
a. Uses Harmonic Mean Sample Size $=5.000$

