

UNIVERSITI TUN HUSSEIN ONN MALAYSIA

FINAL EXAMINATION SEMESTER I SESSION 2021/2022

COURSE NAME

: ACTUARIAL MATHEMATICS II

COURSE CODE

BWA 31503

PROGRAMME CODE

: BWA

EXAMINATION DATE

: JANUARY / FEBRUARY 2022

DURATION

3 HOURS

INSTRUCTION

1. ANSWER ALL QUESTIONS.

2. THIS FINAL EXAMINATION IS AN **ONLINE** ASSESSMENT AND CONDUCTED VIA **OPEN**

BOOK.

THIS QUESTION PAPER CONSISTS OF EIGHT (8) PAGE

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- Q1 (a) Cash value is the amount available in cash upon cancellation of an insurance policy.
 - (i) Identify THREE (3) common insurance options that use the policy's net cash values.

(3 marks)

Discuss the similarities or differences among these three insurance options given (ii) in Q1(a)(i).

(7 marks)

- For a fully discrete whole life insurance of 1,000 on (x), you are given the following: (b)
 - G = 200 is the gross premium.
 - $e_k = 10$, k = 1, 2, 3,... is the per policy expense at the start of year k.
 - $c_k = 0.04, k = 1, 2, 3,...$ is the fraction of premium at the start of year k.

 - $_{10}CV = 1700$ is the cash value payable upon withdrawal at the end of year 4.
 - $q_{x+10}^{(d)} = 0.02$ is the probability of decrement by death.
 - $q_{x+10}^{(w)} = 0.18$ is the probability of decrement by withdrawal. Withdrawals occur at the end of the year.
 - $_{10}$ AS = 1600 is the asset share at the end of year 10.
 - Determine the value of asset share at the end of year 11. (i)

(4 marks)

(ii) If the probability of withdrawal and all expenses for year 11 are each 120% of the values shown above, determine the revised value of the asset share at the end of year 11. Faitulu Saloy Gunzan dun Tesnalogi

(4 marks)

How much does the asset share at the end of year decrease based on Q1(a)(ii)? (iii) (2 marks)

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- Q2 Suppose number of claims S from a motor insurance portfolio follows a Poisson (a) distribution with mean $\lambda = 4.5$. The claim amount distribution is given by p(1) = 0.7and p(2) = 0.3.
 - Construct a table and compute $f_s = Pr(S = x)$ for x = 0, 1, 2, 3, 4, 5. (i)

(10 marks)

Calculate the mean E(N) and variance Var(N) of the number of claims. (ii)

(4 marks)



- (b) Aggregate claims is also known as a random sum with N is the number of claims by a portfolio of insurance policies and X_i is the severity (amount) of claims. Using the same principle, propose a model S as random sum for the following:
 - (i) The number of students denoted as S crossing a certain intersection by car in a given hour.

(3 marks)

(ii) The total amount of rain S that falls at a weather station in a given month.

(3 marks)

Q3 (a) Consider a policy issued at age 35 with an initial gross premium of 1,000 and initial benefit of 120,000. Use the Illustrative Life Table in **Table Q3(a)** with 6% interest to determine the excess first-year expense allowance and the fifth-year reserve.

Table Q3(a): Illustrative Life Table

Age	l_x	d_x	$1,000q_x$
30	95 013.79	145.2682	1.5289
31	94 868.53	152.6317	1.6089
32	94 715.89	160.6896	1.6965
33	94 555.20	169.5052	1.7927
34	94 385.70	179.1475	1.8980
35	94 206.55	189.6914	2.0136
36	94 016.86	201.2179	2.1402
37	93 815.64	213.8149	2.2791
38	93 601.83	227.5775	2.4313
39	93 374.25	242.6085	2.5982
40	93 131.64	259.0186	2.7812
41	92 872.62	276.9271	2.9818
42	92 595.70	296.4623	3.2017
43	92 299.23	317.7619	3.4427
44	91 981.47	340.9730	3.7070
45	91 640.50	366.2529	3.9966

(10 marks)

(b) Five years after issue, the policyholder in **Q3(a)** wishes to change the policy to Term Insurance to age 65 with a coverage of 150,000. Determine the contract premium after the change.

(10 marks)

Q4 (a) Ahmad aged is 50.5 at valuation date. He receives RM6,000 in salary in the month to the valuation date. Ahmad salary increases yearly on 1 January and he is planning to retire at age 65. Assume the replacement ratio is 65% and valuation date of 1 September. Using **Table Q4(a)**,



Table	04(0)	Hypothetica	Salary Scale
1 abie	U4(a):	Hypothetica	Salary Scale

Age	S_X	x	S_X
30	1.00	50	3.41
31	1.06	51	3.63
32	1.13	52	3.86
33	1.20	53	4.10
34	1.28	54	4.35
35	1.36	55	4.62
36	1.44	56	4.91
37	1.54	57	5.21
38	1.63	58	5.53
39	1.74	59	5.86
40	1.85	60	6.21
41	1.96	61	6.56
42	20.9	62	6.93
43	2.22	63	7.31
44	2.36	64	7.70
45	2.51	65	8.08
46	2.67	66	8.48
47	2.84	67	8.91
48	3.02	68	9.35
49	3.21	69	9.82

- determine the salary that Ahmad receives over the year of age $\left(49\frac{5}{6},50\frac{5}{6}\right)$, (i) (1 marks)
- (ii) calculate the expected salary in Ahmad final year of work, (5 marks)
- (iii) calculate Ahmad target pension benefit per year.

Jabatan Matematik dan Slabims (3 marks) Fax util Sains Gunaan dan Testraing

(b) Suppose Fasha aged 30 is a newly hired employee of DRB Group. She receives RM80,000 in her first year of service at the company. Assuming

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- Fasha salary increases 3% per year,
- she receives merit increases of 5% at each of the first three (3) employment anniversaries,
- the pension benefit formula is 1% of the final five (5) year average salary per year service.
- If Fasha retires at age 65, predict the projected final FIVE (5) year average (i) salary. TERBUKA

(5 marks)

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BWA 31503

(ii) Forecast the projected pension benefit Fasha will receive at age 65.

(2 marks)

(iii) Compute the employee's replacement ratio.

(4 marks)

- Q5 A Lexis diagram provides a convenient way of showing the relationship between periods and cohorts. Demographic events can be viewed either by calendar time, age or cohort.
 - (a) Using the Lexis diagram in Figure Q5(a), calculate
 - (i) the age difference between the oldest and the youngest employees at time -25, (3 marks)
 - (ii) the number of employees who have attained age 35 while active in the workforce,

(1 marks)

(iii) the number of employees at time -25, who have attained or will attain age 50 while in the workforce.

(1 marks)

(b) The generation force of mortality at age x for those born at time u is denoted by

$$\mu(x,u) = -\frac{1}{l(x,u)} \frac{\partial}{\partial x} l(x,u).$$

From **Figure Q5(b)**, use the double integral method to show that the number of lives that will attain age x_0 between times t_0 and $t_0 + 1$ and die before time $t_0 + 3$ is given by

$$\int_{t_0}^{t_0+1} l(x_0, y-x_0) dy - \int_{x_0+2}^{x_0+3} l(w, t_0+3-w) dw.$$

(10 marks)

(c) A population density function is defined by

$$l(x,u)=b(u)s(x,u).$$

Let

$$b(u) = 100[1 - e^{-u/100}]$$
 $u > 0$
 $s(x) = e^{-x/100}$ $x > 0$.

Calculate the number of individuals between ages 25 and 50 at time 100.

(5 marks)

-END OF QUESTIONS-

5



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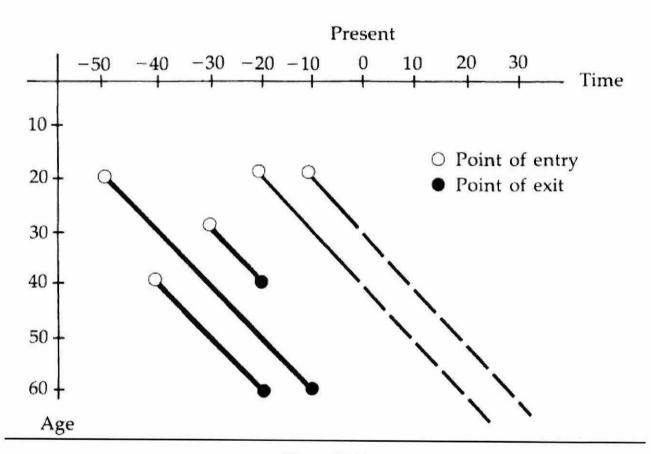


Figure Q5(a)

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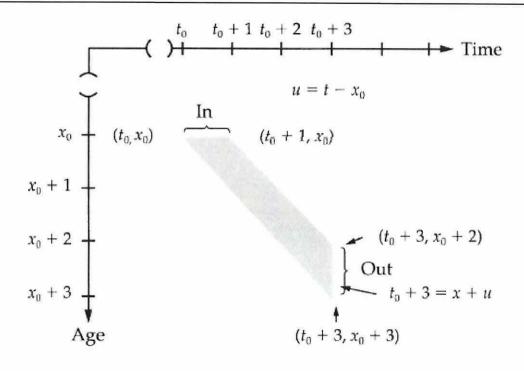


Figure Q5(b)

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FORMULAE

$$\Pr(N=n) = \frac{\lambda^n e^{-\lambda}}{n!}$$

$$\ddot{a}_{x:\overline{n}|} = \sum_{k=0}^{n-1} v^k \cdot {}_k p_x$$

$$A_{x,n}^{1} = \sum_{k=0}^{n-1} v^{k+1} \cdot {}_{k} p_{x} \cdot q_{x+k}$$

$$_{n}E_{x}=v^{n}_{n}P_{x}$$

$$v^n = \frac{1}{\left(1+i\right)^n}$$

$$_{k}P_{x} = \frac{l_{40+k}}{l_{40}}$$

$$-_{0}V = P - \upsilon q_{x}b$$

$$_{k}V = \frac{_{0}V + P\ddot{a}_{x\overline{k}} - bA_{x\overline{k}}^{1}}{_{k}E_{x}}$$

$$_{k+g}V' = \frac{{}_{k}V' + P'\ddot{a}_{x+k}\overline{g}| - b'A_{x+k}^{1}\overline{g}|}{{}_{g}E_{x+k}}$$

$$\int_{t_{0}}^{t_{1}} I(x,t-x)dt$$

$$\int_{x_0}^{x_1} l(x, t_0 - x) dx$$

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