



**UNIVERSITI TUN HUSSEIN ONN MALAYSIA**

**FINAL EXAMINATION  
SEMESTER 2  
SESSION 2022/2023**

COURSE NAME : CONTROL ENGINEERING

COURSE CODE : BDA 30703

PROGRAMME CODE : BDD

EXAMINATION DATE : JULY/AUGUST 2023

DURATION : 3 HOURS

INSTRUCTION

1. ANSWER **ALL** QUESTIONS IN PART A AND ONLY **ONE (1)** QUESTION IN PART B.
2. THIS FINAL EXAMINATION IS CONDUCTED VIA CLOSED BOOK.
3. STUDENTS ARE **PROHIBITED** TO CONSULT THEIR OWN MATERIAL OR ANY EXTERNAL RESOURCES DURING THE EXAMINATION CONDUCTED VIA CLOSED BOOK.

THIS QUESTION PAPER CONSISTS OF NINE (9) PAGES

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**PART A: ANSWER ALL QUESTION**

- Q1** (a) As a newly hired engineer, you are requested to setup a measurement system for measuring liquid temperature in a tank.
- i. Draw a block diagram describing all the elements of the measurement system.
  - ii. List at least four factors that must be taken into consideration in choosing the most suitable instrument for the measurement system.
  - iii. Propose a suitable temperature sensor to be used in the measurement system and describe its working principle with the help of an appropriate illustration.
- (12 marks)
- (b) **Figure Q1(b)** shows e.m.f. temperature characteristic for some standard thermocouple materials. Note that the generated e.m.f. of the thermocouple is too small to be directly used as an input to a data acquisition card which accepts an analog signal of 0 to 24 volt.
- i. Sketch a suitable signal conditioning circuit that can be used to condition the generated e.m.f. of the thermocouple, so that it can be read by the data acquisition card.
  - ii. Derive a general equation relating the input and output of the proposed signal conditioning circuit above.
- (8 marks)

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**Q2** Figure Q2 shows a liquid storage tank system that are commonly used in industries.

- (a) Write all four governing equations of tank 1 (two equations) and tank 2 (two equations) in time-domain. (4 marks)
- (b) Use Laplace transform and converts each governing equations obtained in Q2(a) into s-domain. (4 marks)
- (c) Draw block diagram for each s-domain governing equations obtained in Q2(b). (4 marks)
- (d) Create block diagram of the entire system by combining each individual block diagram obtained in Q2(c). (4 marks)
- (e) Reduce the block diagram obtain in Q2(d) to obtain transfer function of the entire system relating the volumetric flow rate,  $q_i$  to liquid level  $h_2$  in the second tank. (4 marks)

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**Q3** Simplified equations describing the dynamics of a DC motor rotating a disk are given below:

$$T(t) = K_t i_a(t) \quad (1)$$

$$e_b(t) = K_b \omega(t) \quad (2)$$

$$T(t) - T_d(t) = J \frac{d\omega(t)}{dt} + c\omega(t) \quad (3)$$

$$e_a(t) - e_b(t) = R_a i_a(t) \quad (4)$$

where

$\omega(t)$	motor speed
$i_a(t)$	motor current
$T(t)$	motor torque
$T_d(t)$	disturbing torque
$e_d(t)$	back emf voltage
$e_a(t)$	input voltage to motor
$R_a$	motor resistance
$J$	combined inertia of motor and disk
$c$	viscous damping coefficient
$K_t$	motor constant
$K_b$	motor constant

- (a) Derive the transfer function that relates the motor speed,  $\Omega(s)$ , to both the input voltage,  $E_a(s)$ , and the disturbing torque,  $T_d(s)$ . (8 marks)
- (b) Assume  $R_a=1$ ,  $K_t=2$ ,  $K_b=1$ ,  $J=5$ ,  $c=2$ , and that all units of measure are consistent. Show that motor speed increases with the input voltage and reduces with the disturbing torque. Assume unit steps for both the input voltage and the disturbing torque. (4 marks)
- (c) Assume  $R_a=1$ ,  $K_t=2$ ,  $K_b=1$ ,  $J=5$ , and in this part  $c=0$  and  $T_d(t)=0$ , i.e. no viscous friction nor disturbing torque. Show how the motor current changes with time if a constant input voltage,  $e_a(t)=1$ , is applied to the system. Here you need to find and sketch the time response. Be sure to specify the steady-state motor current on the plot. (8 marks)

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**Q4** A company has hired you to study an existing control system designed by a previous control engineer. The control system consists of a second-order system and a proportional controller as shown in **Figure Q4**. Your job is to improve the control system so that the output,  $c(t)$ , follows the input,  $r(t)$ , with no overshoot and no steady-state error. However, the previous engineer forgot to document her/his work, so you don't know the system parameters or the controller gain. So, the first step is to familiarize yourself with the performance of the current system. You apply a step input to the closed-loop system, i.e.,  $r(t) = 1$ . The actual response,  $c(t)$ , is shown in **Figure Q4**. Using the information in the figure:

- (a) Estimate the system parameters,  $\zeta$  and  $\omega_n$  as well as the controller gain,  $K_p$ . (10 marks)
- (b) Sketch the root locus plot as the controller gain is increased from  $K_p = 0$  till  $K_p = \infty$ . (5 marks)
- (c) Determine the range of  $K_p$  to keep the closed-loop system stable. (5 marks)

**PART B : ANSWER ONE(1) QUESTION ONLY**

**Q5** (a) Transfer function of an electric regulator system is given by;

$$G(s) = \frac{200,000s - 2,000,000}{(s^2 + 20s)(s^2 + 20s + 10,000)}$$

Rewrite the transfer function in constituent elementary factors form (2 marks)

- (b) Calculate the magnitude values (dB) and phase values (Degrees) for each constituent element at frequency between 0.01 and 10,000 rad/s. (5 marks)
- (c) Sketch on a semilog graph paper the Bode diagram for the system by using straight line asymptote methods. (10 marks)
- (d) Determine the gain margin (GM) and phase margin (PM) from the Bode plot and relate these values with the stability of the system. (3 marks)

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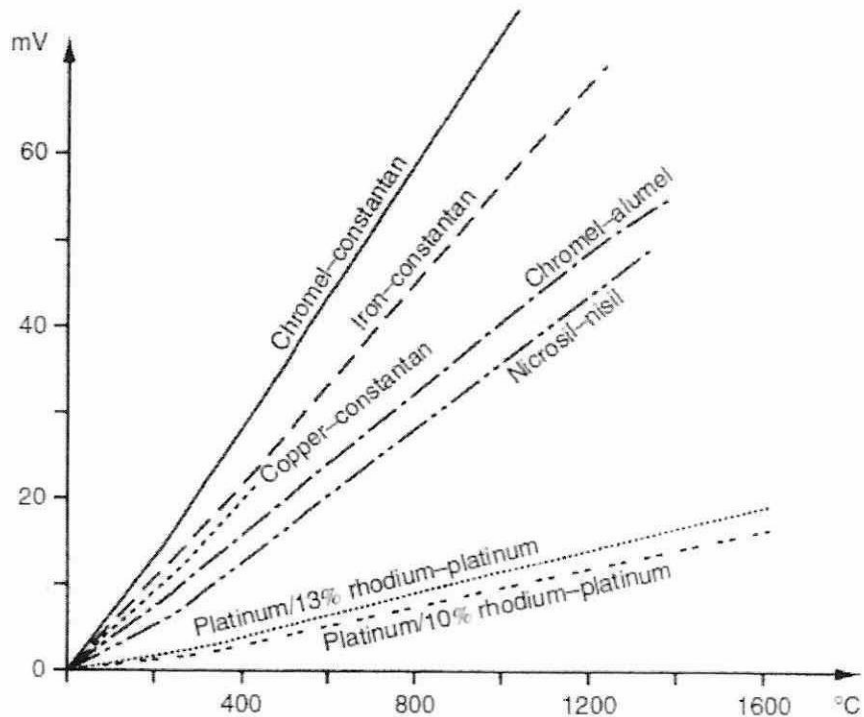
- Q6** (a) Considering a typical feedback control system, explain ONE advantage of a (P+I) controller as compared to a purely proportional (P) controller. (3 marks)
- (b) Illustrate the compensation characteristics of cascade PI and PD compensators. (7 marks)
- (c) Consider the control system shown in **Figure Q6**. Examine a Ziegler-Nichols tuning rule for the determination of the values of parameters  $K_p$ ,  $T_i$  and  $T_d$ . (10 marks)

-END OF QUESTIONS-

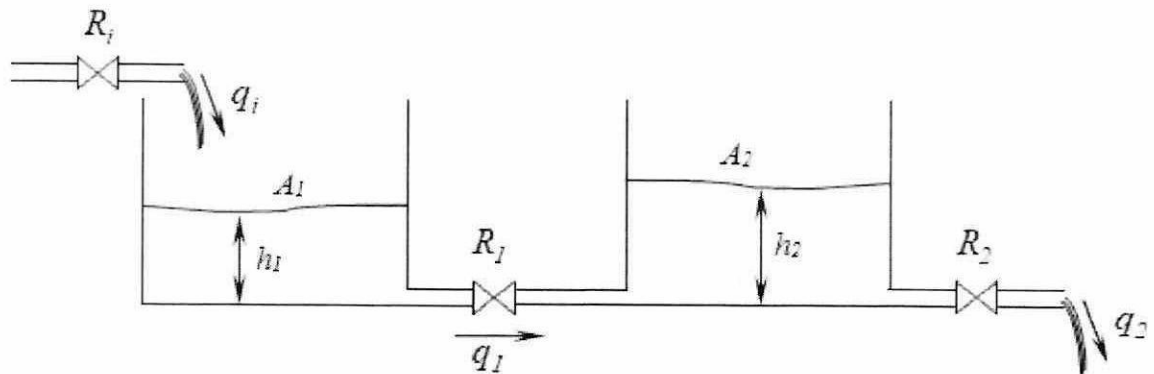
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**Figure Q1(b)**



- $A_1$  = tank 1 surface area
- $A_2$  = tank 2 surface area
- $R_i$  = input valve resistance
- $R_1$  = connecting valve resistance
- $R_2$  = output valve resistance

**Figure Q2**

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FINAL EXAMINATION

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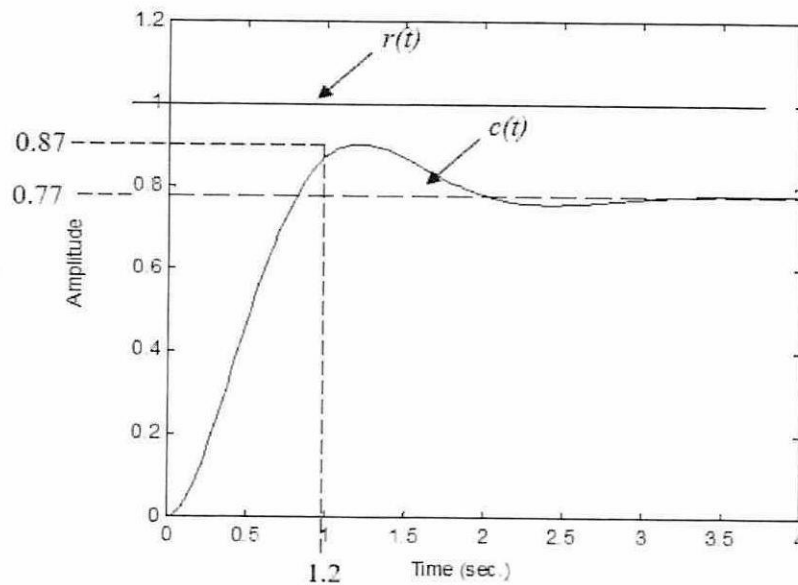
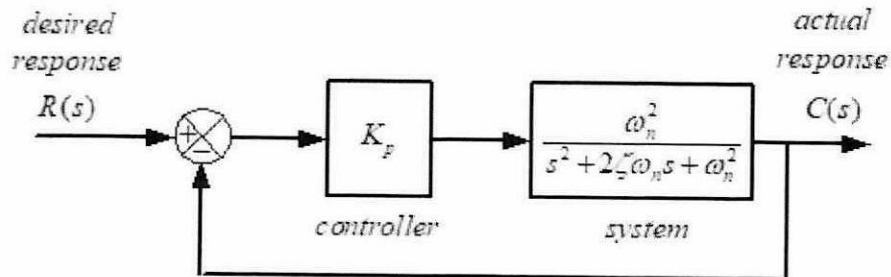


Figure Q4

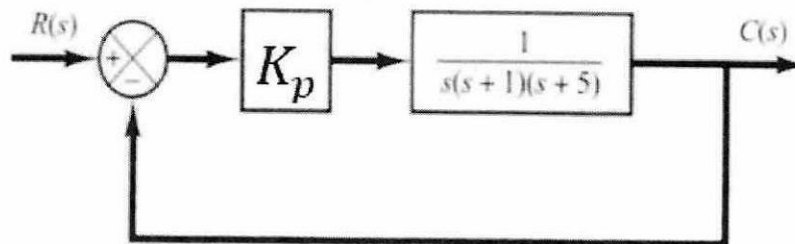


Figure Q6

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**FINAL EXAMINATION**

SEMESTER / SESSION : SEM II / 2022/2023      PROGRAMME CODE : BDD  
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References:

Original	Image	Original	Image
$a$	$\frac{a}{s}$	$\sin(\omega t)$	$\frac{\omega}{s^2 + \omega^2}$
$t$	$\frac{1}{s^2}$	$\cos(\omega t)$	$\frac{s}{s^2 + \omega^2}$
$t^2$	$\frac{2}{s^3}$	$\sinh(\omega t)$	$\frac{\omega}{s^2 - \omega^2}$
$t^n, n \in \mathbb{N}$	$\frac{n!}{s^{n+1}}$	$\cosh(\omega t)$	$\frac{s}{s^2 - \omega^2}$
$e^{at}$	$\frac{1}{s-a}$	$t \sin(\omega t)$	$\frac{2s\omega}{(s^2 + \omega^2)^2}$
$te^{at}$	$\frac{1}{(s-a)^2}$	$t \cos(\omega t)$	$\frac{s^2 - \omega}{(s^2 + \omega^2)^2}$
$t^2 e^{at}$	$\frac{2}{(s-a)^3}$	$e^{at} \sin(\omega t)$	$\frac{\omega}{(s-a)^2 + \omega^2}$
$t^n e^{at}, n \in \mathbb{N}$	$\frac{n!}{(s-a)^{n+1}}$	$e^{at} \cos(\omega t)$	$\frac{s-a}{(s-a)^2 + \omega^2}$

$$C(s) = \frac{\omega_n^2}{s^2 + 2\zeta\omega_n s + \omega_n^2} \quad \zeta = \frac{-\ln(\%OS/100)}{\sqrt{\pi^2 + \ln^2(\%OS/100)}} \quad \%OS = 100e^{-\left(\frac{\zeta\pi}{\sqrt{1-\zeta^2}}\right)}$$

$$T_s = \frac{\pi}{\omega_n \sqrt{1-\zeta^2}} = \frac{\pi}{\omega_d} \quad T_z = \frac{4}{\zeta\omega_n} = \frac{4}{\sigma_d}$$

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