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Universiti Tun Hussein Onn Malaysia

UNIVERSITI TUN HUSSEIN ONN MALAYSIA

**FINAL EXAMINATION
SEMESTER II
SESSION 2016/2017**

COURSE NAME : ENGINEERING MATHEMATICS I
COURSE CODE : DAS 10303
PROGRAMME : DAE
EXAMINATION DATE : JUNE 2017
DURATION : 3 HOURS
INSTRUCTION : SECTION A) ANSWER ALL
QUESTIONS

SECTION B) ANSWER THREE (3)
QUESTIONS ONLY

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THIS QUESTION PAPER CONSISTS OF TEN (10) PAGES

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SECTION A

Q1 (a) Find the Inverse Laplace transform for the functions below.

(i) $F(s) = \frac{2017}{s}$. (1 mark)

(ii) $F(s) = \frac{594}{s-8}$. (2 marks)

(iii) $F(s) = \frac{4}{s^2 + 16} + \frac{20}{s^2 - 100}$. (3 marks)

(iv) $F(s) = \frac{8}{9(s-10)} - \frac{2}{5(s+1)^3}$. (4 marks)

(b) Given $Z(s) = \frac{123}{s^2 + s - 156}$.

(i) Factorize $s^2 + s - 156$. (2 marks)

(ii) Find the partial fractions for $Z(s)$. (4 marks)

(iii) Determine the inverse Laplace transform of $Z(s)$. (4 marks)

Q2 Solve the differential equation below by using Laplace transform.

(a) $y'' - 3y' + 2y = e^{-3t}$, $y(0) = 1$, $y'(0) = 0$ (10 marks)

(b) $y'' - 4y = \sinh t$, $y(0) = 0$, $y'(0) = 0$ (10 marks)

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SECTION B

Q3 (a) Use vertical line test to determine whether the graph shown in **Figure Q3(a)** is a function. Justify your answer.

(2 marks)

(b) Given $f(x) = \begin{cases} x+1, & x < 2 \\ x^2, & x \geq 2 \end{cases}$.

(i) Calculate the value of $f(5)$ and $f(0)$.

(3 marks)

(c) Sketch the graph and determine the domain and range of the following:

(i) $f(x) = \frac{1}{x+2} - 4$.

(4 marks)

(ii) $f(x) = -|x+3| + 5$.

(4 marks)

(d) Given $f(x) = \frac{x}{2} + 1$, $g(x) = x^3$ and $h(x) = -\frac{3}{x+1}$. Find

(i) f^{-1} .

(3 marks)

(ii) $h \circ f \circ g$.

(4 marks)

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Q4 (a) Based on Figure Q4(a), find the limit of $h(x)$ if exist.

(i) $\lim_{x \rightarrow -1^-} h(x).$ (1 mark)

(ii) $\lim_{x \rightarrow -1^+} h(x).$ (1 mark)

(iii) $\lim_{x \rightarrow 3^+} h(x).$ (1 mark)

(b) Given $f(x) = \begin{cases} x^2 & 0 < x < 1 \\ 1 & 1 \leq x < 2 \\ 2 & x = 2 \end{cases}$

(i) Sketch the graph of $f(x).$ (2 marks)

(ii) State at which point $f(x)$ is continuous? (1 mark)

(c) Calculate

(i) $\lim_{x \rightarrow 9} \frac{3 - \sqrt{x}}{9 - x}.$ (3 marks)

(ii) $\lim_{x \rightarrow 3} \frac{x^3 - 5x^2 + 6x}{x^2 - 3x}.$ (3 marks)

(iii) $\lim_{x \rightarrow \infty} \frac{x^5 - 6x^2 - 2x}{2x^5 + 5x - 7}.$ (3 marks)

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(d) Find the values of x which f is not continuous.

(i) $f(x) = \frac{x-1}{x^2 + 4x - 5}.$ (3 marks)

(ii) $f(x) = \frac{3}{x-1}.$

(2 marks)

- Q5** (a) Given a function $f(x) = -3x^4 + x^3 + 8x^2 + 14$. Find all the derivatives $f''(x)$ and $f'''(x)$ of the function.

(2 marks)

- (b) Differentiate function below.

(i) $y = 10x^4 - 3\sqrt{x}$.

(2 marks)

(ii) $y = e^{\cos(x)-2x}$.

(3 marks)

(iii) $y = (\cos x + 5x)(4e^x + \tan x)$.

(4 marks)

- (c) Let $y = \frac{7 \ln x}{x^2 - 2}$, find $\frac{dy}{dx}$ at $x=1$.

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(4 marks)

- (d) Given a function $2x^2 + 4y^3 + 12 = 6x + 5y$,

- (i) Use implicit differentiation to find $\frac{dy}{dx}$.

(3 marks)

- (ii) Find $\frac{dy}{dx}$ at $x=2$ and $y=1$.

(2 marks)

- Q6** (a) A spherical balloon is to be deflated of a rate $x \text{ cm}^3 \text{s}^{-1}$. The radius of the balloon is decreasing at a rate of 0.6 cms^{-1} when its volume is $288\pi \text{ cm}^3$. Find the value of x .

(5 marks)

- (b) Consider the function $f(x) = x^3 - 8x^2 + 16x$.

- (i) Find the critical points.

(5 marks)

- (ii) Find the interval(s) where the function is increasing or decreasing. Hence determine the extremum points.

(6 marks)

(c) Evaluate $\lim_{x \rightarrow 1} \frac{e^{x-1} - x}{x^2 - 2x + 1}$ by using L'Hopital's Rule.
(4 marks)

Q7 (a) Find the Laplace transforms for the functions below.

(i) $f(t) = \sin 5t - 2 \cos t.$
(2 marks)

(ii) $f(t) = 3t - t^2 + 2e^{5t}.$
(2 marks)

(iii) $f(t) = \sinh 3t - \cosh 4t$
(2 marks)

(b) By using First Shift Theorem or Multiply with t^n method, find the Laplace transforms for the functions below.

(i) $f(t) = e^{-2t} \sin 5t .$
(3 marks)

(ii) $f(t) = 2t^2 \cosh t .$
(6 marks)

(c) Find the inverse Laplace transforms for function below.

$$F(s) = \frac{8s + 7}{8s^2 + 6s - 35}.$$

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(5 marks)

- END OF QUESTION -

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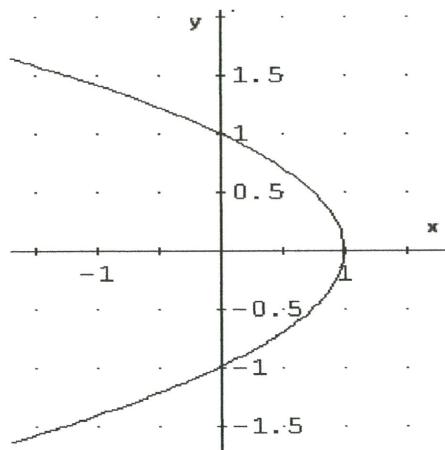


Figure Q3(a)

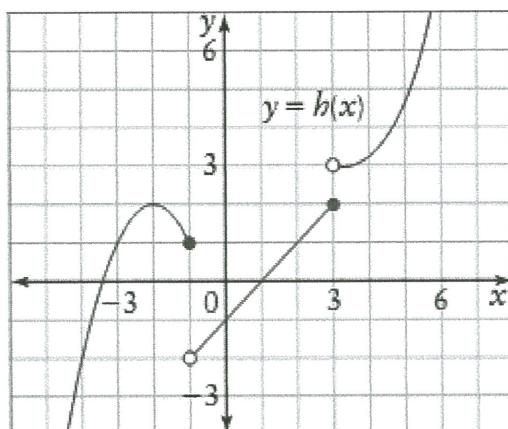


Figure Q4(a)

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Formulae**Differentiation**

$$\frac{d}{dx}(ax^n) = nax^{n-1}$$

$$\frac{d}{ds}(\sin u) = \cos u \cdot \frac{du}{dx}$$

$$\frac{d}{dx}(u^n) = nu^{n-1} \cdot \frac{du}{dx}$$

$$\frac{d}{ds}(\cos u) = -\sin u \cdot \frac{du}{dx}$$

$$\frac{d}{dx}\left(\frac{1}{\sqrt{u}}\right) = \frac{1}{2\sqrt{u}} \cdot \frac{du}{dx}$$

$$\frac{d}{ds}(\tan u) = \sec^2 u \cdot \frac{du}{dx}$$

$$\frac{d}{dx}(e^u) = e^u \cdot \frac{du}{dx}$$

$$\frac{d}{ds}(\sec u) = \sec u \cdot \tan u \cdot \frac{du}{dx}$$

$$\frac{d}{dx}(\ln u) = \frac{1}{u} \cdot \frac{du}{dx}$$

$$\frac{d}{ds}(\cot u) = -\csc^2 u \cdot \frac{du}{dx}$$

$$\frac{d}{dx}(ku) = k \cdot \frac{du}{dx}$$

$$\frac{d}{ds}(\csc u) = -\csc u \cdot \cot u \cdot \frac{du}{dx}$$

$$\frac{d}{dx}(uv) = uv' + vu'$$

$$\frac{d}{dx}\left(\frac{u}{v}\right) = \frac{vu' - uv'}{v^2}$$

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$$\frac{dy}{dx} = \frac{dy/dt}{dx/dt} = \frac{dy}{dt} \times \frac{dt}{dx}$$

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Laplace and Inverse Laplace Transforms

$$L\{f(t)\} = \int_0^{\infty} f(t)e^{-st} dt = F(s)$$

$f(t)$	$F(s)$
k	$\frac{k}{s}$
$t^n, n = 1, 2, ..$	$\frac{n!}{s^{n+1}}$
e^{at}	$\frac{1}{s-a}$
$\sin at$	$\frac{a}{s^2 + a^2}$
$\cos at$	$\frac{s}{s^2 + a^2}$
$\sinh at$	$\frac{a}{s^2 - a^2}$
$\cosh at$	$\frac{s}{s^2 - a^2}$

The First Shift Theorem

$e^{at} f(t)$	$F(s-a)$
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Multiply with t^n

$t^n f(t), n=1,2,..$	$(-1)^n \frac{d^n F(s)}{ds^n}$
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The Unit Step Function

$H(t-0)$	$\frac{1}{s}$
$H(t-a)$	$\frac{e^{-as}}{s}$


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The Second Shift Theorem

$$f(t-a)H(t-a)$$

$$e^{-as}F(s)$$

Heaviside Function

$$g(t) = g_1 + [g_2 - g_1]H(t-a) + [g_2 - g_1]H(t-b)$$

Initial Value Problem

$$L\{y(t)\} = Y(s)$$

$$L\{y'(t)\} = sY(s) - y(0)$$

$$L\{y''(t)\} = s^2Y(s) - sy(0) - y'(0)$$

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