



UNIVERSITI TUN HUSSEIN ONN MALAYSIA

**FINAL EXAMINATION
SEMESTER II
SESSION 2016/2017**

COURSE NAME : FOUNDATION ENGINEERING
COURSE CODE : BFC 43103
PROGRAMME CODE : BFF
EXAMINATION DATE : JUNE 2017
DURATION : 3 HOURS
INSTRUCTION : ANSWER ALL QUESTIONS IN
SECTION A, AND ANY THREE (3)
QUESTIONS IN SECTION B

THIS QUESTION PAPER CONSISTS OF FOURTEEN (14) PAGES

SECTION A

- Q1** (a) Soil improvement and ground modification techniques are used to improve poor/unsuitable subsurface soils and/or to improve the performance of embankments or structures. **Table 1** shows the category of the ground improvement techniques and its methods to carry it out. List **ONE (1)** function for each category of the ground improvement techniques.

(6 marks)

- (b) Mechanical modification and hydraulic modification are methods for improving the ground. List **FOUR (4)** purposes of ground improvement.

(4 marks)

- (c) An embankment is required to be built for a road surface overlaying a clay layer. Site investigation report shows that the clay layer is normally consolidated with two way drainage and has a thickness, H_c of 6 m. The soil properties for this clay are found to have $C_c = 0.27$, $e_o = 1.02$, $c_v = 0.52$ m²/month. It is calculated that the current average effective overburden pressure on the clay is 110 kN/m².

Due to the construction of the embankment on the clay, it is estimated that the increase in vertical effective stress, $[\Delta\sigma'_{(p)}]$ will be about 35 kN/m². To increase the rate of consolidation settlement, a surcharge $[\Delta\sigma'_{(f)}]$ of 30 kN/m² is further placed. **Table 2** shows the variation of degree of consolidation with time factor.

- (i) Due to the addition of the embankment, determine the primary consolidation settlement of the clay layer, $\Delta\sigma'_{(p)}$ and the surcharge $\Delta\sigma'_{(f)}$.

(4 marks)

- (ii) Determine the time required for 80% of the primary consolidation settlement under the addition of both the embankment and surcharge $\Delta\sigma'_{(f)}$.

(5 marks)

- (iii) Determine the “additional” temporary surcharge, $\Delta\sigma'_{(f)}$, that will be required to eliminate the entire primary consolidation settlement calculated in **Q1(c)(i)** above within 6 months using the preloading technique.

(6 marks)

SECTION B

- Q2** (a) A Shelby tube sampler has an outer diameter of 75 mm and wall thickness of 1.7 mm. Determine the area ratio of the tube, and give comments whether the tube could be used for obtaining undisturbed or disturbed soil samples. Briefly explain the difference between the characteristics of the soil for undisturbed samples and disturbed samples. (5 marks)
- (b) You as an experience engineer from an established Geotechnical firm are to be interviewed by representatives of the owner of a site, where a high rise building is to be constructed concerning a subsurface investigation at the site. Discuss the various factors that govern the sub soil exploration, bringing out the guiding principles for deciding the location of boreholes in engineering project. (8 marks)
- (c) Another method of soil investigation is by doing in-situ testing and/or field testing. This is done to obtain direct measurements of the soil properties and its Geotechnical parameters. Explain in detail with the aid of sketches the function advantage and disadvantage of the vane shear test (VST). (12 marks)
- Q3** (a) A strip footing having a width, B of 3 m is constructed at a depth of 2 m below the ground surface in a soil having a cohesion $c = 30\text{kN/m}^2$ and angle of shearing resistance $\phi = 25^\circ$. The water table is at a depth of 5 m below ground level. The dry unit weight of soil above the water table is 17.25 kN/m^3 .
- (i) Determine the ultimate bearing capacity of the soil using the General Bearing Capacity equation. (6 marks)
- (ii) Calculate the net bearing capacity. (3 marks)
- (iii) Calculate the net allowable bearing pressure (Factor of Safety of 3). (3 marks)
- (b) It is known that the total settlement for shallow foundations may control the allowable bearing capacity of the soil.
- (i) State and explain in detail the differences between elastic settlement and consolidation settlement. (3 marks)
- (ii) Explain the process of primary and secondary phases of consolidation. (6 marks)

- (c) **Figure Q3(c)** indicates the construction of a shallow foundation that sustains a 200 kN load on top of a 3 m thick saturated normally consolidated clay. The soil parameter obtained from site investigation are given as, $\gamma_{sat} = 17 \text{ kN/m}^3$, $e_o = 0.8$, $E_s = 6000 \text{ kN/m}^2$, $C_c = 0.32$, $\mu_s = 0.5$, $C_s = 0.09$, $D_f = 2$. Calculate the stress increase in the clay and find the consolidation settlement by using **Table 4** to assist in your calculations.

(7 marks)

- Q4** (a) Piles are structural members that are important in providing support to a superstructure. It can be made out of various types of material and in any cross sectional shape. Categorise the piles according to the types of material used, the type of cross sectional geometry, method of installation and its load transfer mechanism.

(8 marks)

- (b) A pile with a diameter of 500 mm is embedded in clay. The pile extends to a depth of up to 12 m into the ground. The effective pile length for shear resistance is 10 m. The dry unit weight of the clay is 18 kN/m^3 . The water table is located at a depth of 2 m and the saturated unit weights of the clay is 20 kN/m^3 . The recorded undrained shear strength (C_u) profile for the ground is shown in **Table 5**.

- (i) What is the ultimate bearing capacity of the pile with the skin friction factor λ of 0.15.

(8 marks)

- (ii) What is the safe load of the pile when the factor of safety are as follows;

Overall factor of safety	= 2.5
Factor of safety on bearing	= 3.0
Factor of safety on shaft friction	= 1.1

(3 marks)

- (c) Using the group efficiency formula, estimate whether a 3 x 4 rectangular group pile is efficient or not where the centre-to-centre spacing is 1.5 m between the piles. The dimension of the pile is 300 mm x 300 mm in cross section.

(6 marks)

- Q5**
- (a) Conventional retaining walls can be generally classified into four types. Describe with the aid of sketches **THREE (3)** of them and outline the ways in which such retaining walls may fail. (6 marks)
- (b) An anchored sheet pile wall retains 6.4 m of cohesionless soil that has a unit weight of 16 kN/m^3 and a 30° angle of friction. Surface of the soil is level with the top of the wall. The anchor tie rods are installed at a depth of 1.2 m below the top of the wall and are spaced 3 m apart horizontally. Friction on the surface of the piling is negligible. Assuming “free earth support”;
- (i) Design the sheet pile wall by calculating the actual depth of penetration (12 marks)
- (ii) Determine the tension in a single anchor tie rod (7 marks)

-END OF QUESTIONS-

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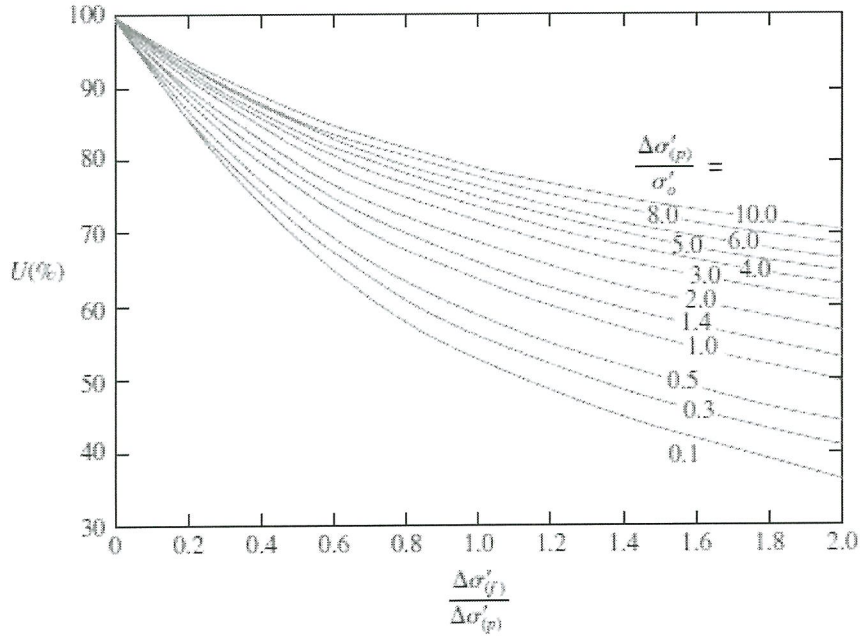


Figure Q2(c)

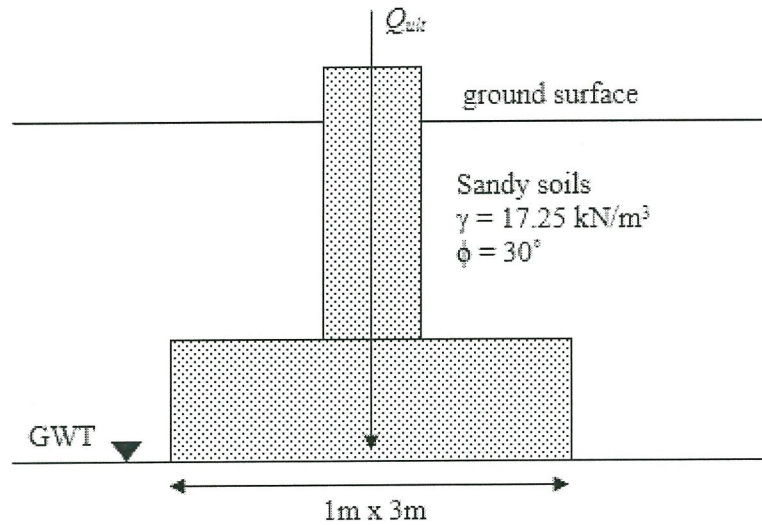


Figure Q3(c)

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Table 3: Bearing Capacity Factors for Shallow Foundations

ϕ'	Terzhagi's Method						Meyerhof's Method		
	General Shear			Local Shear					
	N_c	N_q	N_γ	N_c	N_q	N_γ	N_c	N_q	N_γ
0	5.70	1.00	0.00	5.70	1.00	0.00	5.14	1.00	0.00
1	6.00	1.10	0.01	5.90	1.07	0.005	5.38	1.09	0.07
2	6.30	1.22	0.04	6.10	1.14	0.02	5.63	1.20	0.15
3	6.62	1.35	0.06	6.30	1.22	0.04	5.90	1.31	0.24
4	6.97	1.49	0.10	6.51	1.30	0.055	6.19	1.43	0.34
5	7.34	1.64	0.14	6.74	1.39	0.074	6.49	1.57	0.45
6	7.73	1.81	0.20	6.97	1.49	0.10	6.81	1.72	0.57
7	8.15	2.00	0.27	7.22	1.59	0.128	7.16	1.88	0.71
8	8.60	2.21	0.35	7.47	1.70	0.16	7.53	2.06	0.86
9	9.09	2.44	0.44	7.74	1.82	0.20	7.92	2.25	1.03
10	9.61	2.69	0.56	8.02	1.94	0.24	8.35	2.47	1.22
11	10.16	2.98	0.69	8.32	2.08	0.30	8.80	2.71	1.44
12	10.76	3.29	0.85	8.63	2.22	0.35	9.28	2.97	1.69
13	11.41	3.63	1.04	8.96	2.38	0.42	9.81	3.26	1.97
14	12.11	4.02	1.26	9.31	2.55	0.48	10.37	3.59	2.29
15	12.86	4.45	1.52	9.67	2.73	0.57	10.98	3.94	2.65
16	13.68	4.92	1.82	10.06	2.92	0.67	11.63	4.34	3.06
17	14.60	5.45	2.18	10.47	3.13	0.76	12.34	4.77	3.53
18	15.12	6.04	2.59	10.90	3.36	0.88	13.10	5.26	4.07
19	16.56	6.70	3.07	11.36	3.61	1.03	13.93	5.80	4.68
20	17.69	7.44	3.64	11.85	3.88	1.12	14.83	6.40	5.39
21	18.92	8.26	4.31	12.37	4.17	1.35	15.82	7.07	6.20
22	20.27	9.19	5.09	12.92	4.48	1.55	16.88	7.82	7.13
23	21.75	10.23	6.00	13.51	4.82	1.74	18.05	8.66	8.20
24	23.36	11.40	7.08	14.14	5.20	1.97	19.32	9.60	9.44
25	25.13	12.72	8.34	14.80	5.60	2.25	20.72	10.66	10.88
26	27.09	14.21	9.84	15.53	6.05	2.59	22.25	11.85	12.54
27	29.24	15.90	11.60	16.30	6.54	2.88	23.94	13.20	14.47
28	31.61	17.81	13.70	17.13	7.07	3.29	25.80	14.72	16.72
29	34.24	19.98	16.18	18.03	7.66	3.76	27.86	16.44	19.34
30	37.16	22.46	19.13	18.99	8.31	4.39	30.14	18.40	22.40

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Table 4: Variation of I_c with m_1 and n_1

n_1	m_1									
	1	2	3	4	5	6	7	8	9	10
0.20	0.994	0.997	0.997	0.997	0.997	0.997	0.997	0.997	0.997	0.997
0.40	0.960	0.976	0.977	0.977	0.977	0.977	0.977	0.977	0.977	0.977
0.60	0.892	0.932	0.936	0.936	0.937	0.937	0.937	0.937	0.937	0.937
0.80	0.800	0.870	0.878	0.880	0.881	0.881	0.881	0.881	0.881	0.881
1.00	0.701	0.800	0.814	0.817	0.818	0.818	0.818	0.818	0.818	0.818
1.20	0.606	0.727	0.748	0.753	0.754	0.755	0.755	0.755	0.755	0.755
1.40	0.522	0.658	0.685	0.692	0.694	0.695	0.695	0.696	0.696	0.696
1.60	0.449	0.593	0.627	0.636	0.639	0.640	0.641	0.641	0.641	0.642
1.80	0.388	0.534	0.573	0.585	0.590	0.591	0.592	0.592	0.593	0.593
2.00	0.336	0.481	0.525	0.540	0.545	0.547	0.548	0.549	0.549	0.549
3.00	0.179	0.293	0.348	0.373	0.384	0.389	0.392	0.393	0.394	0.395
4.00	0.108	0.190	0.241	0.269	0.285	0.293	0.298	0.301	0.302	0.303
5.00	0.072	0.131	0.174	0.202	0.219	0.229	0.236	0.240	0.242	0.244
6.00	0.051	0.095	0.130	0.155	0.172	0.184	0.192	0.197	0.200	0.202
7.00	0.038	0.072	0.100	0.122	0.139	0.150	0.158	0.164	0.168	0.171
8.00	0.029	0.056	0.079	0.098	0.113	0.125	0.133	0.139	0.144	0.147
9.00	0.023	0.045	0.064	0.081	0.094	0.105	0.113	0.119	0.124	0.128
10.00	0.019	0.037	0.053	0.067	0.079	0.089	0.097	0.103	0.108	0.112

Table 5: Variation of C_u with pile embedment length

Depth (m)	0	2	4	7	10	13	16
Undrained shear strength, C_u (kN/m^2)	70	70	70	85	100	115	130

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List of formula

SOIL IMPROVEMENT AND GROUND MODIFICATION

$S_{c(p)} = \frac{C_c H_c}{1 + e_o} \log \frac{\sigma'_o + \Delta\sigma'_{(p)}}{\sigma'_o}$ $S_{c(p+f)} = \frac{C_c H_c}{1 + e_o} \log \frac{\sigma'_o + [\Delta\sigma'_{(p)} + \Delta\sigma'_{(f)}]}{\sigma'_o}$ $U = \frac{\log \left[\frac{\sigma'_o + \Delta\sigma'_{(p)}}{\sigma'_o} \right]}{\log \left[\frac{\sigma'_o + \Delta\sigma'_{(p)} + \Delta\sigma'_{(f)}}{\sigma'_o} \right]}$	$T_v = \frac{c_v t}{H_c^2}$ <p>For U%: 0% to 60%; $T_v = \frac{\pi}{4} \left(\frac{U\%}{100} \right)^2$</p> <p>For U% > 60%; $T_v = 1.781 - 0.931 \log(100 - U\%)$</p> $U = \frac{\log \left[1 + \frac{\Delta\sigma'_{(p)}}{\sigma'_o} \right]}{\log \left[1 + \frac{\Delta\sigma'_{(p)}}{\sigma'_o} \left(1 + \frac{\Delta\sigma'_{(f)}}{\sigma'_{(p)}} \right) \right]}$
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SITE INVESTIGATION

<p style="text-align: center;">Rock quality designation (RQD)</p> <p style="text-align: center;">= $\frac{\Sigma \text{length of recovered pieces equal to or larger than 101.6 mm}}{\text{theoretical length of rock cored}}$</p>	
$A_R(\%) = \frac{D_o^2 - D_i^2}{D_i^2} (\%)$	$N_{corrected} = C_N * N_{field}$ $C_N = 0.77 \log_{10} \frac{1915}{p'_o}$

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SHALLOW FOUNDATIONS

Modification of Bearing Capacity Equations for Water Table

Case I for water within $0 \leq D_1 \leq D_f$; $q = D_1 \gamma_{dry} + D_2 (\gamma_{sat} - \gamma_w)$ $\gamma' = \gamma_{sat} - \gamma_w$	Case II for water within $0 \leq d \leq B$; $q = D_1 \gamma_{dry}$ $\bar{\gamma} = \gamma' + \frac{d}{B} (\gamma_{dry} - \gamma')$	Case III when the water table is located so that $d \geq B$, the water will have no effect on the ultimate bearing capacity.
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$$q_u = c' N_c F_{cs} F_{cd} F_{ci} + q N_q F_{qs} F_{qd} F_{qi} + \frac{1}{2} \gamma B N_\gamma F_{\gamma s} F_{\gamma d} F_{\gamma i}$$

Shape Factor

$F_{cs} = 1 + \frac{B}{L} \cdot \frac{N_q}{N_c}$	$F_{qs} = 1 + \frac{B}{L} \tan \phi$	$F_{\gamma s} = 1 - 0.4 \frac{B}{L}$
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Depth Factor

$D_f/B \leq 1, \text{ for } \phi = 0$

$F_{cd} = 1 + 0.4 (D_f/B)$	$F_{qd} = 1$	$F_{\gamma d} = 1$
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$D_f/B \leq 1, \text{ for } \phi > 0$

$F_{cd} = F_{qd} - \frac{1 - F_{qd}}{N_c \tan \phi'}$	$F_{qd} = 1 + 2 \tan \phi' (1 - \sin \phi')^2 \frac{D_f}{B}$	$F_{\gamma d} = 1$
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$D_f/B > 1, \text{ for } \phi = 0$

$F_{cd} = 1 + 0.4 \tan^{-1} \left(\frac{D_f}{B} \right)$ <small>radians</small>	$F_{qd} = 1$	$F_{\gamma d} = 1$
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$D_f/B > 1, \text{ for } \phi > 0$

$F_{cd} = F_{qd} - \frac{1 - F_{qd}}{N_c \tan \phi'}$	$F_{qd} = 1 + 2 \tan \phi' (1 - \sin \phi')^2 \tan^{-1} \left(\frac{D_f}{B} \right)$ <small>radians</small>	$F_{\gamma d} = 1$
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where L is the length of the foundation and $L > B$.

Inclination Factor

$$F_{ci} = F_{qi} = \left(1 - \frac{\beta^\circ}{90^\circ} \right)^2 \qquad F_{\gamma i} = \left(1 - \frac{\beta}{\phi'} \right)^2$$

β is the inclination of the load on the foundation with respect to vertical

Eccentric Loading in Shallow Foundations

$q_{\max} = \frac{Q}{BL} \pm \frac{6M}{B^2 L}$ $q_{\max} = \frac{4Q}{3L(B - 2e)}$	$e = \frac{M}{Q}$ $FS = \frac{Q_{ult}}{Q}$
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SHALLOW FOUNDATIONS

$$q'_u = c'N_c F_{cs} F_{cd} F_{ci} + qN_q F_{qs} F_{qd} F_{qi} + \frac{1}{2} \gamma' B' N_\gamma F_{\gamma s} F_{\gamma d} F_{\gamma i}$$

One Way Eccentric Loading in Shallow Foundations

Method 1:

$$B' = B - 2e$$

$$L' = L$$

$$q'_u = c'N_c F_{cs} F_{cd} F_{ci} + qN_q F_{qs} F_{qd} F_{qi} + \frac{1}{2} \gamma' B' N_\gamma F_{\gamma s} F_{\gamma d} F_{\gamma i}$$

$$Q_{ult} = q'_u B' L'$$

Method 2:

$$Q_{ult} = B \left[c' N_{c(e)} + q N_{q(e)} + \frac{1}{2} \gamma B N_{\gamma(e)} \right]$$

$$Q_{ult} = BL \left[c' N_{c(e)} F_{cs(e)} + q N_{q(e)} F_{qs(e)} + \frac{1}{2} \gamma B N_{\gamma(e)} F_{\gamma s(e)} \right]$$

$$F_{cs(e)} = 1.2 - 0.025 \frac{L}{B}$$

$$F_{qs(e)} = 1.00$$

$$F_{\gamma s(e)} = 1.0 + \left(\frac{2e}{B} - 0.68 \right) \frac{B}{L} + \left[0.43 - \left(\frac{3}{2} \right) \left(\frac{e}{B} \right) \right] \left(\frac{B}{L} \right)^2$$

Method 3:

$$R_k = 1 - \frac{q_{u(eccentric)}}{q_{u(centric)}}$$

$$R_k = a \left(\frac{e}{B} \right)^k$$

$$q_{u(eccentric)} = q_{u(centric)} (1 - R_k)$$

$$q_{u(centric)} = qN_q F_{qd} + \frac{1}{2} \gamma B N_\gamma F_{\gamma d}$$

$$Q_{ult} = B q_{u(eccentric)}$$

Primary Consolidation Settlement for Normally Consolidated Clays

$$S_{c(p)} = \frac{C_c H_c}{1 + e_o} \log \frac{\sigma'_o + \Delta \sigma'_{av}}{\sigma'_o}$$

Primary Consolidation Settlement for OverConsolidated Clays

for $\sigma'_o + \Delta \sigma'_{av} < \sigma'_c$

$$S_{c(p)} = \frac{C_s H_c}{1 + e_o} \log \frac{\sigma'_o + \Delta \sigma'_{av}}{\sigma'_o}$$

for $\sigma'_o < \sigma'_c < \sigma'_o + \Delta \sigma'_{av}$

$$S_{c(p)} = \frac{C_s H_c}{1 + e_o} \log \frac{\sigma'_c}{\sigma'_o} + \frac{C_c H_c}{1 + e_o} \log \frac{\sigma'_o + \Delta \sigma'_{av}}{\sigma'_c}$$

Average Increase in Pressure

$$\Delta \sigma'_{av} = \frac{1}{6} (\Delta \sigma'_{top} + 4 \Delta \sigma'_{medium} + \Delta \sigma'_{bottom})$$

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PILE FOUNDATIONS

Ultimate Capacity of Piles and Group Piles in Saturated Clay

$$Q_s = \sum f p \Delta L$$

$$f = \beta \sigma'_o$$

$$\beta = K \tan \phi'_R$$

$$K = 1 - \sin \phi'_R$$

$$K = 1 - \sin \phi'_R \sqrt{\text{OCR}}$$

$$\text{OCR} = \frac{p_c}{P_o}$$

$$Q_p = A_p q_p$$

$$Q_p = A_p q N_q^*$$

$$Q_p \approx N_c^* c_u A_p$$

$$Q_p = 9 c_u A_p$$

$$f_{av} = \lambda (\bar{\sigma}'_o + 2 c_u)$$

$$\sum Q_u = n_1 n_2 [9 A_p c_{u(p)} + \sum \alpha p c_u \Delta L]$$

$$L_g = (n_1 - 1) d + 2 \left(\frac{D}{2} \right)$$

$$B_g = (n_2 - 1) d + 2 \left(\frac{D}{2} \right)$$

$$\sum Q_u = L_g B_g c_{u(p)} N_c^* + \sum 2 (L_g + B_g) c_u \Delta L$$

$$\Delta s_{c_i} = \left[\frac{\Delta e_i}{1 + e_{o_i}} \right] H_i$$

$$\eta = \frac{[2(n_1 + n_2 - 2)d + 4D]}{p n_1 n_2}$$

CONVENTIONAL GRAVITY AND CANTILEVER WALL

Rankine's Theory

$$P_a = \frac{1}{2} K_a \gamma_1 H^2$$

$$P_a = \frac{1}{2} K_a \gamma_1 H^2 + q K_a H$$

$$P_v = P_a \sin \alpha^\circ$$

$$P_h = P_a \cos \alpha^\circ$$

$$P_p = \frac{1}{2} K_p \gamma_2 D^2 + 2 c'_2 \sqrt{K_p} D$$

$$K_a = \tan^2 (45^\circ - \frac{1}{2} \phi'_1)$$

$$K_p = \tan^2 (45^\circ + \frac{1}{2} \phi'_2)$$

$$FS_{\text{overturning}} = \frac{\sum M_R}{\sum M_O}$$

$$\sum M_O = P_h \left(\frac{H'}{3} \right)$$

$$P_h = P_a \cos \alpha$$

$$P_v = P_a \sin \alpha$$

$$FS_{\text{sliding}} = \frac{\sum F_{R'}}{\sum F_d} = \frac{(\sum V) \tan(k_1 \phi'_2) + B k_2 c'_2 + P_p}{P_a \cos \alpha}$$

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LATERAL EARTH PRESSURE AND RETAINING WALLS

$K_a = \tan^2 \left(45 - \frac{\phi}{2} \right)$ $K_p = \tan^2 \left(45 + \frac{\phi}{2} \right)$ $L_3 = \frac{\sigma'_2}{\gamma'(K_p - K_a)}$ $\sigma'_5 = (\gamma L_1 + \gamma L_2) K_p + \gamma L_3 (K_p - K_a)$ $A_1 = \frac{\sigma'_5}{\gamma'(K_p - K_a)}$ $A_2 = \frac{8P}{\gamma'(K_p - K_a)}$ $A_3 = \frac{6P \left[2\bar{z}' \gamma'(K_p - K_a) + \sigma'_5 \right]}{\gamma'^2 (K_p - K_a)^2}$	$A_4 = \frac{P \left[6\bar{z}' \sigma'_5 + 4P \right]}{\gamma'^2 (K_p - K_a)^2}$ $L_4^4 + A_1 L_4^3 - A_2 L_4^2 - A_3 L_4 - A_4 = 0$ $\sigma'_4 = \sigma'_5 + \gamma' L_4 (K_p - K_a)$ $\sigma'_3 = L_4 (K_p - K_a) \gamma'$ $L_5 = \frac{\sigma'_3 L_4 - 2P}{\sigma'_3 + \sigma'_4}$ $K_{p(\text{design})} = \frac{K_p}{FS}$
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Free Earth Support

$$K_a = \tan^2 \left(45 - \frac{\phi}{2} \right)$$

$$K_p = \tan^2 \left(45 + \frac{\phi}{2} \right)$$

$$L_3 = \frac{\sigma'_2}{\gamma'(K_p - K_a)}$$

$$\sigma'_8 = \gamma'(K_p - K_a) L_4$$

$$L_4^3 + 1.5L_4^2(l_2 + L_2 + L_3) - \frac{3P[(L_1 + L_2 + L_3) - (\bar{z} + l_1)]}{\gamma'(K_p - K_a)} = 0$$

$$P - \frac{1}{2}[\gamma'(K_p - K_a)]L_4^2 - F = 0$$