

# UNIVERSITI TUN HUSSEIN ONN MALAYSIA

# FINAL EXAMINATION SEMESTER II SESSION 2017/2018

**COURSE NAME** 

ADVANCED STRUCTURAL

**ANALYSIS** 

COURSE CODE

: BFS40103

PROGRAMME CODE

BFF

**EXAMINATION DATE** 

JUNE 2018 / JULY 2018

**DURATION** 

3 HOURS

**INSTRUCTION** 

ANSWER FOUR (4) QUESTIONS

ONLY

TERBUKA

THIS QUESTION PAPER CONSISTS OF **EIGHT (8)** PAGES

#### CONFIDENTIAL

Q1 (a) Figure Q1(a) shows a simply supported beam carrying three concentrated loads at points B, C, and D. Determine the displacement at point C due to all the concentrated loads.

(7 marks)

- (b) An indeterminate frame shown in **Figure Q1(b)** is subjected to a horizontal force of 50 kN at point D and uniformly distributed load of 20 kN/m along member BC. EI for member AB is two times of member BC.
  - (i) Determine the reactions at supports A and C. Take support C as redundant.

(12 marks)

(ii) Sketch the shear force and bending moment diagrams.

(6 marks)

Q2 (a) For the two member truss shown in **Figure Q2(a)**, determine the reaction forces at node 1 and node 3. Given displacement at Joint 2 is:

$$\left\{\begin{array}{c} d_1 \\ d_2 \end{array}\right\} = \left\{\begin{array}{c} 4.505/AE \\ -19.003/AE \end{array}\right\}$$

(14 marks)

(b) Two connected steel bars as shown in **Figure Q2(b)** are axially loaded with 100 N at node 3. The cross section area for bar B is half of bar A. The horizontal displacement at node 2 is half of displacement at node 3. By using finite element method, determine the displacement at node 2 and node 3. The modulus of elasticity is constant.

(11 marks)

Q3 (a) What is the difference between short and slender column?

(5 marks)

- (b) Derive the Euler equation for:
  - i. Column with one end fixed and one end free
  - ii. Column with both ends fixed.

Use sketches to support your answer.

(8 marks)

(c) A column pinned at both ends is as shown in **Figure Q3(c)**. Determine whether the column is slender or not. Assume  $L_e$  /r for slender column is > 30. Given E=23 GPa and safety factor is 2. Determine the safe load for the column.

(12 marks)

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- Q4 The rigid-jointed frame is loaded with working loads as shown in **Figure Q4**.
  - (a) List **THREE** (3) conditions that must be satisfied by a structure in its collapsed state.

(6 marks)

(b) Find the maximum plastic moment, M<sub>p</sub>.

(19 marks)

- Q5 (a) Explain the following terms;
  - (i) Orthotropically reinforced slab
  - (ii) Isotropically reinforced slab

(6 marks)

(b) A rectangular slab, simply supported along all four edges, is isotropically reinforced to give a yield moment of 27kN/m per metre width of slab. The slab measures 8 m by 6 m. By considering a reasonable collapse mode, as shown in **Figure Q5(b)**, calculate the value of the uniformly distributed load, q, that would just cause collapse.

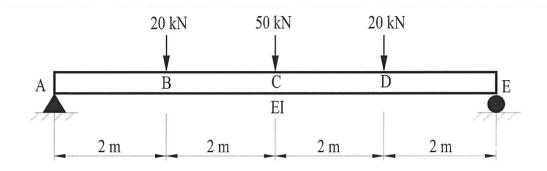
(19 marks)



- END OF QUESTIONS -

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PROGRAMME : 4 BFF



# FIGURE Q1(a)

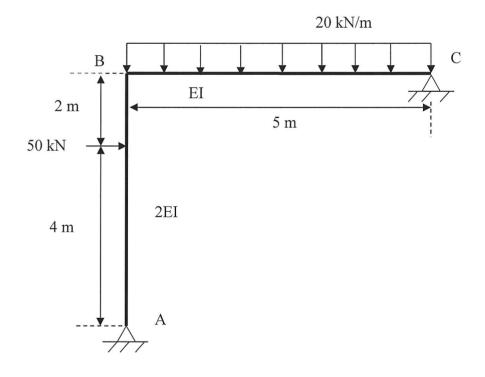
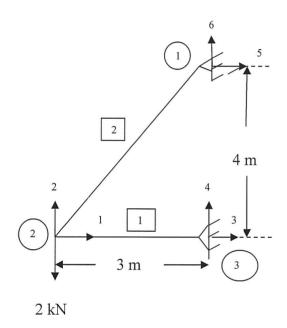


FIGURE Q1(b)



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# FIGURE Q2(a)

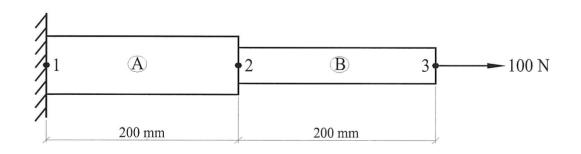
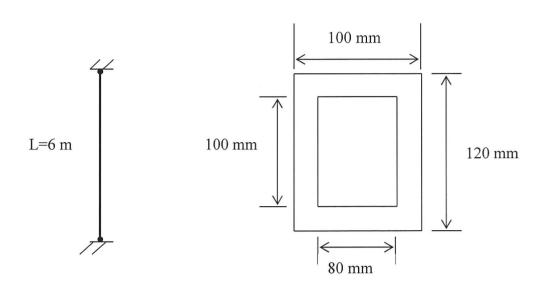


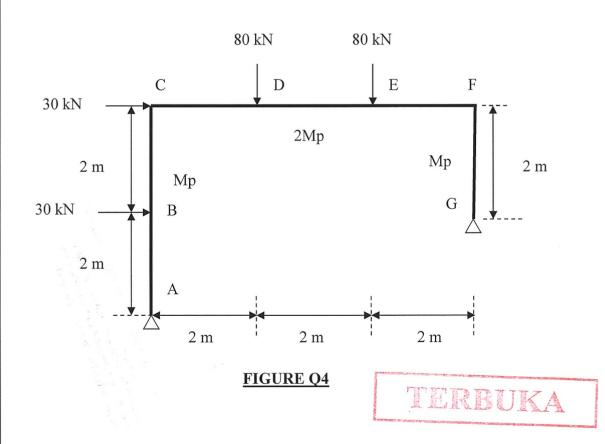
FIGURE Q2(b)



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# FIGURE Q3(c)



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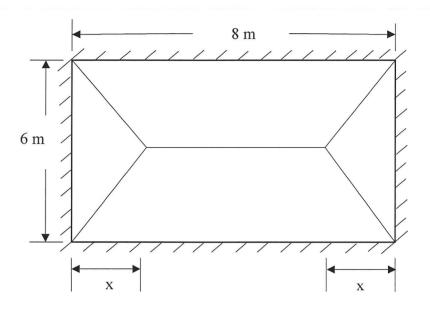


FIGURE Q5(b)

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#### **FORMULA**

# 1) Beam Deflection Formulae

BEAM TYPE	SLOPE AT ENDS	DEFLECTION AT ANY SECTION IN TERMS OF x	MAXIMUM AND CENTER DEFLECTION
6. Beam Simply Supported at Ends – Concentrated load P at the center			
$\begin{array}{c c} \theta, & P & i\theta, & X \\ \hline 0, & \delta_{max} \end{array}$	$\theta_1 = \theta_2 = \frac{Pl^2}{16EI}$	$y = \frac{Px}{12EI} \left( \frac{3l^2}{4} - x^2 \right)$ for $0 < x < \frac{l}{2}$	$\delta_{\max} = \frac{Pl^3}{48EI}$
7. Beam Simply Supported at Ends - Concentrated load P at any point			
*	$\theta_1 = \frac{Pb(l^2 - b^2)}{6lEI}$ $\theta_2 = \frac{Pab(2l - b)}{6lEI}$	$y = \frac{Pbx}{6lEI} (l^2 - x^2 - b^2) \text{ for } 0 < x < a$ $y = \frac{Pb}{6lEI} \left[ \frac{l}{b} (x - a)^3 + (l^2 - b^2) x - x^3 \right]$ for $a < x < l$	$\delta_{\max} = \frac{Pb(l^2 - b^2)^{3/2}}{9\sqrt{3}  lEI} \text{ at } x = \sqrt{(l^2 - b^2)/3}$ $\delta = \frac{Pb}{48EI} (3l^2 - 4b^2) \text{ at the center, if } a > b$
<ol> <li>Beam Simply Supported at Ends – Uniformly distributed load ω (N/m)</li> </ol>			
ω δ <sub>msx</sub>	$\theta_1 = \theta_2 = \frac{\omega l^3}{24EI}$	$y = \frac{\omega x}{24EI} \left( l^3 - 2lx^2 + x^3 \right)$	$\delta_{\max} = \frac{5\omega l^4}{384EI}$
Beam Simply Supported at Ends – Couple moment M at the right end			
0,1 (0, M x	$\theta_1 = \frac{Ml}{6EI}$ $\theta_2 = \frac{Ml}{3EI}$	$y = \frac{Mlx}{6EI} \left( 1 - \frac{x^2}{l^2} \right)$	$\delta_{\text{max}} = \frac{Ml^2}{9\sqrt{3}EI} \text{ at } x = \frac{l}{\sqrt{3}}$ $\delta = \frac{Ml^2}{16EI} \text{ at the center}$
10. Beam Simply Supported at Ends – Uniformly varying load: Maximum intensity ω <sub>c</sub> (N/m)			
$0 = \frac{\Theta_{0}}{l} \times 0$ $V = \frac{\Theta_{0}}{l} \times 0$	$\theta_1 = \frac{7\omega_o l^3}{360EI}$ $\theta_2 = \frac{\omega_o l^3}{45EI}$	$y = \frac{\omega_e x}{360 l EI} \left( 7l^4 - 10l^2 x^2 + 3x^4 \right)$	$\delta_{\text{max}} = 0.00652 \frac{\omega_o l^4}{EI} \text{ at } x = 0.519 l$ $\delta = 0.00651 \frac{\omega_o l^4}{EI} \text{ at the center}$

# **FORMULA**

$$k = \frac{EA}{L} \begin{bmatrix} \lambda_x^2 & \lambda_x \lambda_y & -\lambda_x^2 & -\lambda_x \lambda_y \\ \lambda_x \lambda_y & \lambda_y^2 & -\lambda_x \lambda_y & -\lambda_y^2 \\ -\lambda_x^2 & -\lambda_x \lambda_y & \lambda_x^2 & \lambda_x \lambda_y \\ -\lambda_x \lambda_y & -\lambda_y^2 & \lambda_x \lambda_y & \lambda_y^2 \end{bmatrix}$$

