

UNIVERSITI TUN HUSSEIN ONN MALAYSIA

FINAL EXAMINATION SEMESTER II SESSION 2013/2014

COURSE NAME

BASIC ALGEBRA

(ALJABAR ASAS)

COURSE CODE

BBR 23703

PROGRAMME

3 BBR / 4 BBR

EXAMINATION DATE :

JUNE 2014

DURATION

3 HOURS

INSTRUCTION

ANSWER FIVE (5) QUESTIONS

FROM SIX (6) QUESTIONS

THIS QUESTION PAPER CONSISTS OF FIVE (5) PAGES

CONFIDENTIAL

Q1 (a) Find the sum of the following three polynomials

$$3y^{50} - 2y + y^{40} + 2y^{30} + 5$$
, $-y^{40} - 3y^{30} - 2$ and $2y^{50} + 3y^{30} + 9$

(3 marks)

- (b) Solve $x^2 3x + 2 = 0$ by
 - (i) completing the squares,

(5 marks)

(ii) quadratic formula.

(5 marks)

(b) Given that -1 is the root of $x^3 - 5x^2 - x + 5$. Hence, factorize completely the equation.

(7 marks)

Q2 Given the system of linear equation

$$3x - y + 2z = 4$$

 $-4x - 2y + 4z = -2$
 $x + 2y + 3z = 6$

(a) Write the system above into equation AX = B.

(2 marks)

(b) Find the determinant of matrix A.

(4 marks)

(c) Find the inverse of matrix A.

(12 marks)

(d) Use inversion to solve the system of linear equation.

(2 marks)

Q3 (a) Given that the fifth term of arithmetic sequence is 13 and its thirteenth term is -9. (i) Find the value of first term, a and its common difference, d. (4 marks) (ii) Find the tenth term. (2 marks) (iii) Find the sum from first term until tenth term. (2 marks) A geometric sequence is defined as $30, 20, \frac{40}{3}, \frac{80}{9}, \dots$ (b) (i) Find the value of common ratio, r. (2 marks) (ii) Calculate the tenth term, T_{10} . (2 marks) (iii) The sum for this sequence up to 10 terms, S_{10} . (3 marks) (iv) State whether this series converges or diverges. State your reason. (2 marks) (v) If it is converges, evaluate its summation, S_{∞} . (3 marks) (a) Expand the expression $\frac{1}{\sqrt{(1-2x)^3}}$ until the term of x^3 using Binomial series. Q4 (5 marks) (b) Expand the following expressions until the term of x^3 using Binomial series. (i) $\frac{1}{(1+x)}$. (5 marks) (ii) $\frac{1}{(1+3x)}$. (5 marks)

(5 marks)

(c) From Q4 (b), verify that $\frac{1}{(1+x)(1+3x)} = 1-4x+13x^2-40x^3...$

- **Q5** (a) The function f is given by $f(x) = -x^3 + 4$.
 - (i) Find the value of x such that f(x) = 0.

(2 marks)

(ii) Sketch the graph and determine the domain and range.

(4 marks)

- (b) Given f(x) = 2x 7, $h(x) = x^3 + 4$ and $g(x) = \frac{5}{x 1}$, calculate
 - (i) $f \circ g$, $f \circ g(2)$.

(3 marks)

(ii) $h \circ f, h \circ f(-5)$.

(3 marks)

(iii) the value of c if $h \circ f(c) = -5$

(3 marks)

(c) Functions f and g are defined as $f(x) = e^{2x}$, g(x) = x - 3, $x \in \Re$. Sketch the graph of f(x) and g(x) and determine their domain and range.

(5 marks)

- Q6 (a) For each equation, determine whether the conic section is circle, ellipse or parabola. State your reason.
 - (i) $x^2 + y^2 81 = 0$.

(4 marks)

(ii) $15x^2 - 15y^2 + 20x + 20y = 0$.

(3 marks)

(iii) $x^2 + 5x - 12y + 55 = 0$

(3 marks)

(b) Write the equation for a circle with radius of $2\sqrt{3}$ and center at (2,-2). Write the equation in the form of $ax^2 + bxy + cy^2 + dx + ey + f = 0$. Hence, sketch the circle.

(10 marks)

FINAL EXAMINATION

SEMESTER / SESSION: SEM II 2013/2014 PROGRAMME : 3BBR / 4BBR COURSE : BASIC ALGEBRA COURSE CODE : BBR23703

Polynomial

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

$$p(x) = (x - a)q(x) + r(x)$$

Matrices

$$x = \frac{-b \pm \sqrt{b^2 - 4ac}}{2a}$$

Cofactor, $C_{ij} = (-1)^{i+j} M_{ij}$ (M_{ij} is minor/determinant of the sub-matrix A)

Determinant of **A**,
$$|\mathbf{A}| = \sum_{i=1}^{k} \alpha_{ij} C_{ij}$$

Inverse of A,
$$\mathbf{A} = \frac{1}{|\mathbf{A}|} A dj(\mathbf{A})$$
 where $A dj(\mathbf{A}) = C_{ij}^T$

For
$$AX = B$$
, $X = A^{-1}B$

Arithmetic Series

- (i) The nth term for arithmetic series, $T_n = a + (n-1)d$ where a is the first term and d is the common difference.
- (ii) Common difference, $d = T_{n+1} T_n$.
- (iii) Sum for arithmetic series, $S_n = \frac{n}{2} [2a + (n-1)d]$ or $S_n = \frac{n}{2} [a+l]$.

Geometric Series

- (i) The nth term for geometric series, $T_n = ar^{n-1}$ where a is the first term and r is the common ratio.
- (ii) Common ratio, $r = \frac{T_{n+1}}{T_n}$.
- (iii) Sum for geometric series, $S_n = \frac{a(r^n 1)}{r 1}$, r > 1 or $S_n = \frac{a(1 r^n)}{1 r}$, r < 1.
- (iv) If |r| < 1, then the infinite geometric series converges with its summation, $S_{\infty} = \frac{a}{1-r}$.
- (v) If |r| > 1, then the infinite geometric series diverges.

Binomial Series

$$(1+x)^{r} = 1 + rx + \frac{r(r-1)}{1(2)}x^{2} + \frac{r(r-1)(r-2)}{1(2)(3)}x^{3} + \dots + \frac{r(r-1)(r-2)\dots(r-n+1)}{n!}x^{n}$$